ANALYSIS AND SIMULATION OF THE VARIOUS GENERATORS USED IN WIND SYSTEMS

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Abstract: The world’s energy consumption grows unceasingly, raising important questions about the problem of global warming due to greenhouse gases (GHG), on the one hand, and to the exhaustion of the fossil resources, on the other one. Given this awareness, an economic development that abides by the environmental requirements is absolutely necessary. Wind power is one of the most promising renewable energies. It is within this context that this paper attempts to study the different configurations and performances of the most used generators in wind systems.

Key words: Various Generators, IG, DSIG, DFIG, PSMG, Simulation.

1. Introduction
The search for a lasting development that is complying with the environmental requirements and the imminent exhaustion of fossil energies have contributed to the development of renewable energies in general and wind energy in particular [1]. Within this context, this research work deals with the various generators used in the field of aerogenerators. A classification approach to the various generators used in wind systems will be introduced, and the main configuration of the fixed speed system and that of the variable speed one will be described. The mathematical models and the simulation of the induction generator (IG), the dual-stator windings induction generator (DSIG), the doubly fed induction generator (DFIG) as well as the permanent magnet synchronous generator (PSMG) will be dealt with in details.

2. Induction generator
2.1. Mathematical model
The mathematical model of the induction generator in the quasi-stationary reference frame ($\alpha$-$\beta$) are given as [2-4]

$$[B][U] = [A][I] + \omega_t [C][I] + [L]\frac{d}{dt}[I]$$

with,

$$[U] = [v_{\alpha}, v_{\beta}, 0, 0]^T$$

$$[I] = [i_{\alpha}, i_{\beta}, i_{\sigma}, i_{fb}]^T$$

and

$$\frac{d}{dt}[I] = \frac{d}{dt}[I]$$

$$[B] = \text{diag}([-1, -1, 0, 0])$$

$$[A] = \text{diag}[r_s, r_s, r_r, r_r];$$

$$[C] =$$

$$
\begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & L_m & 0 & L_r \\
-L_m & 0 & -L_r & 0
\end{bmatrix}
$$

$$[L] =$$

$$
\begin{bmatrix}
L_{\alpha\alpha} & L_{\alpha\beta} & L_{\alpha\sigma} & L_{\alpha fb} \\
L_{\alpha\beta} & L_{\beta\beta} & L_{\beta\sigma} & L_{\beta fb} \\
L_{\alpha\sigma} & L_{\beta\sigma} & L_{\sigma\sigma} & L_{\sigma fb} \\
L_{\alpha fb} & L_{\beta fb} & L_{\sigma fb} & L_{fb fb}
\end{bmatrix}
$$

where,

$r_s$ and $r_r$ are respectively the per phase stator resistance and the per phase rotor resistance;

$v_{\sigma}$ and $i_{\sigma}$ are respectively the "$\alpha$" components of the stator voltages and currents;

$v_{fb}$ and $i_{fb}$ are respectively the "$\beta$" components of the stator voltages and currents;

$i_{\sigma}$ and $i_{fb}$ are respectively the "$\sigma$" and "$fb$" components of the rotor currents;

$L_m$ is the magnetizing inductance;

That under linear magnetic conditions $L_{\alpha\alpha} = 0$, $L_{\alpha\sigma} = L_{\alpha fb} = L_m$, $L_{\beta\beta} = L_{\beta fb} = L_r$ and $L_{\sigma\sigma} = L_{fb fb}$.

The saturation effect is taken into account by the expression of the magnetizing inductance $L_m$ with respect to the magnetizing current $i_m$ defined as [5]

$$i_m = \sqrt{(i_{\alpha\sigma} + i_{\alpha fb})^2 + (i_{\beta\sigma} + i_{\beta fb})^2}$$

To express $L_m$ with respect to $i_m$, we use a polynomial approximation is given by

$$L_m = 0.3308 - 0.0099i_m - 0.0074i_m^2 + 0.0006i_m^3$$

(3)
The electromagnetic torque is evaluated as [6-8]

\[ T_{em} = \frac{3}{2} P L_m (i_{\beta r} l_{ar} - i_{\alpha r} l_{br}) \]  

(4)

\( P \) is number of pole pairs.

The mechanical equation which remains the same for all generators is described as

\[ J \frac{d\Omega}{dt} = T_{sh} - T_{em} \]  

(5)

where,

\( \Omega \) is the mechanical speed \((\Omega = \omega_r/P)\);

\( T_{sh} \) is the shaft torque;

\( J \) is the moment of inertia.

2.2 Resistive-inductive load model

General resistive-inductive passive load is represented in the quasi-stationary reference frame as the IG with the following equations

\[
\begin{align*}
   p v_{\alpha s} &= (1/C) (i_{\alpha s} - i_{\alpha sl}) \\
   p i_{\alpha sl} &= (1/L_s) (v_{\alpha s} - R_s i_{\alpha sl}) \\
   p v_{\beta s} &= (1/C) (i_{\beta s} - i_{\beta sl}) \\
   p i_{\beta sl} &= (1/L_s) (v_{\beta s} - R_s i_{\beta sl})
\end{align*}
\]  

(6)

where,

\( p \) denotes differentiation w.r.t time;

\( i_{\alpha sl} \) and \( i_{\beta sl} \) are respectively the "\( \alpha \)" and "\( \beta \)" components of the currents flowing into excitation capacitor;

\( C \) is the excitation capacitance;

\( R_s \) is the load resistance;

\( L_s \) is the load inductance.

2.3 Simulation results and discussion

The simulations in this paper have been developed in MATLAB/SIMULINK® environment. In the model the prime mover speed and the excitation capacitance are fixed at \( \Omega_r = 157.5 \text{rad/s} \) and \( C = 62 \mu \text{F/phase} \) respectively. The induction generator parameters used in the simulation are given in the Appendix.

Inserting the load leads to a decrease of the level of all the IG characteristics in comparison with those observed without a load (prior to inserting it), which are 8.18\% at the level of the stator voltage (Fig. 1), 6.66\% of the stator current (Fig. 2) and 16.82\% of the magnetization current (Fig. 3). This is essentially due to the demagnetization of the machine and to the lack of reactive energy which is necessary for both magnetizing the machine and supplying the load, notably the one that is inductive and energy consuming, and it is up to the excitation capacitors to satisfy and share the energy that they produce between the two consumers of the reactive power. Fig. 4 shows the variation of the load current at resistive-inductive load, which stabilizes at 1.34A.
3. Dual-stator windings induction generator

3.1. Mathematical model

The mathematical model of the dual-stator windings induction generator in the synchronous reference frame (d-q) is given as [9, 11]

$$[B][U] = [A][I] + \omega_L[C][I] + [L][\bar{I}]$$

(7)

with,

$$[U] = [v_{d1} \ v_{q1} \ v_{d2} \ v_{q2} \ v_{dr} \ v_{qr}]^T;$$

$$[I] = [i_{d1} \ i_{q1} \ i_{d2} \ i_{q2} \ i_{dr} \ i_{qr}]^T;$$

$$[B] = \text{diag}[1 \ 1 \ 1 \ 1 \ 0 \ 0];$$

$[A]$, $[C]$ and $[L]$ are respectively given by matrices (8), (9) and (10), where $L_{sl}$, $L_{qr}$ and $\omega_L$ are defined as:

$$L_{sl} = L_{slm} + L_{sm}, \quad L_{qr} = L_{qrm} + L_{qm}$$

and $\omega_L = \omega - \omega_r$;

$\omega_r$ is the speed of the synchronous reference frame;

$v_{d1}$, $v_{q1}$, $v_{d2}$, $v_{q2}$, $v_{dr}$ and $v_{qr}$ are respectively the "d" components of the stator voltages and currents;

$i_{d1}$, $i_{q1}$, $i_{d2}$ and $i_{q2}$ are respectively the "q" components of the stator voltages and currents;

$v_{dr}$, $i_{dr}$ and $\psi_{rd}$ are respectively the "d" components of the rotor voltage, current and flux linkage;

$v_{qr}$, $i_{qr}$ and $\psi_{rq}$ are respectively the "q" components of rotor voltage, current and flux linkage;

$$\psi_{rd} \quad \text{and} \quad \psi_{rq}$$

are respectively the magnetizing current $|i_m|$ and the per phase rotor resistance;

$L_{md}$ and $L_{mq}$ are respectively the direct and quadrature magnetizing inductance.

That under linear magnetic conditions $L_{md} = L_{mq} = L_m$ and $L_{sl} = 0$.

$L_m$ is the steady state saturated inductance and is given by [10]

$$L_m = 0.1406 + 0.0014i_{m} - 0.0012i_{m}^2 + 0.00005i_{m}^3$$

(11)

The magnitude of the magnetizing current $|i_m|$ is calculated as

$$i_m = \sqrt{(-i_{d1} - i_{d2} + i_{dr})^2 + (-i_{q1} - i_{q2} + i_{qr})^2}$$

(12)

The electromagnetic torque is evaluated as [11, 12]

$$T_{em} = \frac{3}{2} p \frac{L_m}{L_r} \left( i_{q1} + i_{q2} \right) \psi_{dr} - \left( i_{d1} + i_{d2} \right) \psi_{qr}$$

(13)

3.2. Resistive-inductive load model

General resistive-inductive passive load is represented in the synchronous reference frame as the DSIG with the following equations

$$p \nu_{d1} = \left( \frac{1}{C_{sl}} \right) \left( i_{d1} - i_{d1l} \right) + \omega_L v_{q1}$$

$$p \nu_{d1l} = \left( \frac{1}{C_{sl}} \right) \left( i_{d1l} - R_1 i_{d1l} + \omega_L i_{q1l} \right)$$

(14)

$$[A] = \begin{bmatrix}
-r_1 & -\omega_L (L_{1q} + L_{q}) & 0 & 0 & 0 & 0 \\
-\omega_L (L_{1q} + L_{q}) & -r_1 & -\omega_L L_{dq} & 0 & 0 & 0 \\
0 & \omega_L L_{dq} & -r_2 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
-L_{md} & -L_{md} & 0 & L_{r} + L_{md} & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
\end{bmatrix}
$$

(9)

$$[C] = \begin{bmatrix}
-L_{1d} & 0 & 0 & 0 & 0 & 0 \\
0 & -L_{1d} & L_{dq} & 0 & 0 & 0 \\
-L_{dq} & -L_{dq} & 0 & (L_{2q} + L_{q}) & 0 & 0 \\
-L_{md} & -L_{md} & 0 & 0 & L_{r} + L_{md} & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 \\
\end{bmatrix}
$$

(10)
\[
\begin{align*}
\begin{cases}
 pv_{q_1} &= (1/C_{sh1})(i_{q_1} - i_{q1L}) - \omega_e v_{d1} \\
 pi_{d1L} &= (1/L_1)(v_{d1} - R_{d1L}i_{d1L} - \omega_L i_{q1L}) \\
 pv_{d2} &= (1/C_{sh2})(i_{d2} - i_{d2L}) + \omega_e v_{q2} \\
 pi_{d2L} &= (1/L_2)(v_{d2} - R_{d2L}i_{d2L} + \omega_L i_{q2L}) \\
 pv_{q2} &= (1/C_{sh2})(i_{q2} - i_{q2L}) - \omega_e v_{d2} \\
 pi_{q2L} &= (1/L_2)(v_{q2} - R_{q2L}i_{q2L} - \omega_L i_{d2L}) 
\end{cases}
\end{align*}
\]

where,

- \( C_{sh1} \) and \( C_{sh2} \) are respectively the excitation capacitance connected to the dual stator windings set I and II;
- \( R_1 \) and \( R_2 \) are respectively the load resistances connected across the windings set I and II;
- \( L_1 \) and \( L_2 \) are respectively the load inductances connected across the windings set I and II;
- \( i_{d1L} \), \( i_{d2L} \), and \( i_{q2L} \) are respectively the "d" and "q" components of the load current.

### 3.3. Simulation results and discussion

In the model the prime mover speed (\( \Omega_r \)) and the excitation capacitance are fixed at 157 rad/s, and \( C_{sh1} = C_{sh2} = 40 \mu F/phase \) respectively. The dual-stator windings induction generator parameters used in the simulation are given in the Appendix.

Figs. 5, 6 and 7 show the variation of the stator voltage, the stator current and the magnetizing current of the dual-stator windings of induction generator sets I respectively. Figs 8 and 9 show the variation of the load current of the DSIG sets I and II respectively. At \( t = 3s \), the three-phase star load (resistive-inductive load (\( R_1 = R_2 = 200 \Omega \) and \( L_1 = L_2 = 0.05 \ H \)) is applied, the generated voltage, the stator current and the magnetizing current decrease respectively to 35.26\%, 34.98\% and 42.58\% regarding to the values at no load.

Application of the load, as the case of classical induction generator, causes the decrease of the voltage generated by the decrease of the magnetizing current. Furthermore, the introduce of an inductive load generate more important decrease of reactive power.

![Fig. 5. Variation of the DSIG voltage (\( v_{s1} \) (V) phase \( s \)) at resistive-inductive load.](image)

![Fig. 6. Variation of the DSIG current (\( i_{s1L} \) (A) phase \( s \)) at resistive-inductive load.](image)

![Fig. 7. Variation of the DSIG magnetizing current (\( i_{m1} \) (A) phase \( s \)) at resistive-inductive load.](image)

![Fig. 8. Variation of the DSIG load current (\( i_{s1} \) (A) phase \( s \)) at resistive-inductive load.](image)

![Fig. 9. Variation of the DSIG load current (\( i_{s2L} \) (A) phase \( s \)) at resistive-inductive load.](image)
4. Doubly fed windings induction generator

4.1. Mathematical model

The mathematical model of the doubly fed induction generator in the synchronous reference frame (d-q) are given as [13-15]

\[
[B][U] = [A][I] + \omega_d[C][I] + [L][I]
\]

with, \([U] = [v_{ds}, v_{qs}, v_{dr}, v_{qr}]^T\);

\[
[I] = [i_{ds}, i_{qs}, i_{dr}, i_{qr}]^T
\]

\[
[B] = \text{diag}[1, 1, 1, 1] ;
\]

\[
[A] = \begin{bmatrix}
-r_d & \omega_d L_d & 0 & -\omega_d L_m \\
-\omega_d L_d & -r_d & \omega_d L_m & 0 \\
0 & 0 & -r_r & 0 \\
0 & 0 & 0 & -r_r
\end{bmatrix};
\]

\[
[C] = \begin{bmatrix}
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & L_m & 0 & -L_r \\
-L_m & 0 & L_r & 0
\end{bmatrix};
\]

\[
[L] = \begin{bmatrix}
-L_s & 0 & 0 & 0 \\
0 & -L_s & 0 & L_s \\
L_s & 0 & 0 & 0 \\
0 & -L_m & 0 & L_m
\end{bmatrix};
\]

where, \(L_s\) and \(L_r\) are respectively the total stator and rotor inductances;

The electromagnetic torque is expressed as [16, 17]

\[
T_{em} = \frac{3}{2} P \frac{L_m}{L_s} (i_{qs} \psi_{ds} - i_{ds} \psi_{qs})
\]

4.2. Resistive load model

General resistive passive load is represented in the synchronous reference frame (d-q) as the DFIG with the following equations

\[
\begin{align*}
v_{ds} &= R_s i_{ds} \\
v_{qs} &= R_s i_{qs}
\end{align*}
\]

4.3. Simulation results and discussion

In the model the prime mover speed (\(\Omega_r\)) is fixed at 106rad/s. The DFIG parameters used in the simulation are given in the Appendix.

Figs. 10, 11, 12 and 13 show respectively the variation of the stator voltage, the rotor voltage, the stator current and the rotor current of the doubly fed induction generator outflows on a resistive load (\(R_L = 100\Omega\)).

At the start, the generated stator voltage (\(v_{sa}(V)\)) and stator current (\(i_{sa}(A)\)) increase in an exponential way during a few fractions of milliseconds, then they respectively stabilize at 2.176V and at 9.05A and at a rate of flow totally established at \(t = 0.158s\); then they continue their progress with constant amplitudes knowing that the frequency is kept constant.

The rotor voltage (\(v_{ra}(V)\)) progresses in a sinusoidal way and with amplitude that is equal to \(12\sqrt{2}V\) and in a frequency periodic of 2Hz. The rotor current (\(i_{ra}(A)\)) stabilizes right at the second alternation. Then, it evolves in a sinusoidal way with constant amplitude that is approximately at 9.05A, and with a frequency that is identical to that of the rotor voltage.

The various characteristics of the DFIG functioning show that the transitional speed is of a very short duration.
5. Permanent magnet synchronous generator

5.1. Mathematical model

The mathematical model of the permanent magnet synchronous generator in the rotor frame \((x-y)\) is given as \([18, 19]\)

\[
[B][U] = [A][I] + \omega_0 [C][I] + [L][I] + \omega_0 [D] \phi_f
\]  \hspace{1cm} (21)

with,

\[U = \begin{bmatrix} v_{x_1} \\ v_{y_1} \end{bmatrix};
\]

\[I = \begin{bmatrix} i_{x_1} \\ i_{y_1} \end{bmatrix};
\]

\[B = \text{diag} \begin{bmatrix} 1 \\ 1 \end{bmatrix};
\]

\[A = \begin{bmatrix} -r_s \\ r_s \end{bmatrix};
\]

\[L = \text{diag} \begin{bmatrix} L_{x_1} \\ L_{y_1} \end{bmatrix};
\]

\[D = \begin{bmatrix} 0 \\ 0 \end{bmatrix};
\]

\[C = \begin{bmatrix} 0 & -L_{y_1} \\ -L_{x_1} & 0 \end{bmatrix}.
\]

where, \(v_{x_1}, v_{y_1}, i_{x_1}, i_{y_1}\) are respectively the "x" and "y" components of the stator voltages and currents; \(L_{x_1}\) and \(L_{y_1}\) are respectively the direct and quadrature of the total stator inductances; \(\phi_f\) is the flux produced by the permanent magnets. The electromagnetic torque is expressed as \([20, 21]\)

\[
T_{em} = \frac{3}{2} P \left( L_{x_1} i_{x_1} i_{y_1} + \phi_f i_{y_1} \right)
\]  \hspace{1cm} (22)

5.2. Resistive-inductive load model

General resistive-inductive passive load is represented in the rotor frame \((x-y)\) as the PMSG with the following equations

\[
\begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} -(r_s + R_L) & -\omega_0 L_{q_1} \\ \omega_0 L_{x_1} & -(r_s + R_L) \end{bmatrix} \begin{bmatrix} i_{x_1} \\ i_{y_1} \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{d}{dt} \phi_f \end{bmatrix} - \begin{bmatrix} 0 \\ -L_{x_1} + L_{q_1} \end{bmatrix} \begin{bmatrix} i_{x_1} \\ i_{y_1} \end{bmatrix}
\]  \hspace{1cm} (23)

with,

\[
\begin{align*}
v_{x_1} &= R_s i_{x_1} + L_{x_1} \frac{d}{dt} i_{x_1} \\
v_{y_1} &= R_s i_{y_1} + L_{q_1} \frac{d}{dt} i_{y_1}
\end{align*}
\]  \hspace{1cm} (24)

5.3. Simulation results and discussion

In the model the prime mover speed \((\Omega_r)\) is fixed at 314 rad/s. The permanent magnet synchronous generator parameters used in the simulation are given in the Appendix.

Figs. 14, 15, 16 and 17 show the variation of the stator voltage, the stator current, the direct stator current and the quadrature stator current of the permanent magnet synchronous generator outflows on a resistive-inductive load \((R_L = 42\Omega \text{ and } L_L = 0.159H)\). The results achieved demonstrate clearly that:

The current following the \((i_{x_1}(A))\) direct axis stabilizes at \(-0.15A\) staring from \(t = 0.051s\). The in squaring one is \(i_{y_1} = 7.37A\) when beyond \(t = 0.035s\). This leads us to conclude that the duration of the transitional speed is very short.

The stator current \((i_{w_1}(A))\) which moves through the load takes a sinusoidal form and evolves in a uniform way and with a constant amplitude starting from the second alternation \((t = 0.025s)\), its utmost value is equal to 7.37A.

The stator voltage \((v_{w_1}(V))\) reaches its maximal value of 482.6V at \(t = 0.022s\) (second period), and continues its evolution in exactly the same way as the stator current \((i_{w_1}(A))\).

The stator current \((i_{w_1}(A))\) is out of phase to the rear in comparison with the voltage, which is due to the presence of the inductive charge and also to the inductive nature of the machine.
6. Interpretation

Considering the simulation tasks done during the last years within the LEB research laboratory on the various generators previously studied, we can conclude that the induction generators constitute 85% of the wind applications, for a power range between 100kW and 1MW. The dual-stator windings induction generator, dealt with only recently, constitute a serious rival to the induction generator. The doubly fed induction generator is widespread in the great power range. It constitutes, along with the permanent magnet synchronous generator, one of the two competing solutions in variable speed wind generators.

7. Conclusion

This paper has outlined the results achieved by the simulation of the various generators that are most commonly used in the aerodynamic conversion systems that function autonomously and which outflow on static charges. The latter influence the generators which work with a fixed speed (IG and DSIG), because it is up to the excitation capacities to share the reactive energy that they produce between the load, notably the inductive one, and for the magnetization of the machine. Conversely, electrical generators working with a variable speed (DFIG and PSMG) remain unchanged with regard to the load.

The field of renewable energies, notably wind energies, is a new opportunity for research in electrical engineering. These research works will be fruitful and multidisciplinary enough to meet the requirements of these complex systems.

8. Appendix

The machine parameters used in the simulation are as follows:

1. IG parameters:
   - Stator resistance $r_s = 3.38 \Omega$;
   - Stator leakage inductance $L_{ls} = L_{o} = 0.324 H$;
   - Rotor resistance $r_r = 3.38 \Omega$;
   - Rotor leakage inductance $L_{lr} = L_{o} = 0.324 H$;
   - Moment of inertia $J = 0.005 Kg.m^2$;
   - Number of poles pair $P = 2$.

2. DSIG parameters:
   - Stator resistances per-phase (winding set I and II) $r_1 = r_2 = 1.9 \Omega$;
   - Stator leakage inductances per-phase (winding set I and II) $L_{1o} = L_{2o} = 0.0132 H$;
   - Rotor per-phase resistance $r_1 = 2.1 \Omega$;
   - Rotor per-phase leakage inductance $L_{lr} = 0.0132 H$;
   - Common mutual leakage inductance $L_{lm} = 0.01 H$;
   - Moment of inertia $J = 0.038 Kg.m^2$;
   - Number of poles pair $P = 2$.

3. DFIG parameters:
   - Stator resistance $r_s = 0.95 \Omega$;
   - Stator leakage inductance $L_{s} = 0.094 H$;
   - Rotor resistance $r_r = 1.8 \Omega$;
   - Rotor leakage inductance $L_{r} = 0.088 H$;
   - Mutual leakage inductance $L_{mr} = 0.082 H$;
   - Moment of inertia $J = 0.1 Kg.m^2$;
   - Number of poles pair $P = 3$.

4. PSMG parameters:
   - Stator resistance $r_s = 0.6 \Omega$;
   - Direct stator leakage inductance $L_{s} = 0.0014 H$;
   - Quadrature stator leakage inductance $L_{q} = 0.0028 H$;
   - Flux produced by the permanent magnets $\phi_f = 1 Wb$;
   - Number of poles pair $P = 1$.

References