DESIGN AND ANALYSIS OF BUCK BOOST CONVERTER BASED LED DRIVER FOR ENHANCING THE STABILITY

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Abstract—This paper develops a light emitting diode (LED) driver circuit based on buck-boost converter including parasitic resistance. The transfer function analysis of buck boost converter and whole system has been obtained by considering parasitic resistance of the component because the resistance of an LED varies with temperature, making the circuit unstable. The forward bias of the LED used was 3.0V~4.5V, and the forward current was 0.6A. Ten 3W white-light LEDs were driven in series in the proposed circuit. In an LED only 15% to 25% of electrical energy is converted into light; the rest is converted into heat, which increases its temperature. In some typical application like designing of lighting system for underground coalmines this change in resistance can cause hazardous effect. Hence, LED must be operated at constant current for constant illumination for at least 10-12 hours without failure. Therefore, a closed-loop control system has been designed in this paper to increase output voltage stability. The driver circuit is operated in continuous buck-boost mode and the results are then simulated using PSIM software. The transfer function analysis has been done by using averaging method. For, stability analysis MATLAB and PSIM software has been used and it has been observed that phase margin is 93.8°.

Keywords: buck-boost, closed-loop, stabilizer, LED, transfer function.

1. INTRODUCTION

In general the power management of a LED can be divided into two main parts, namely, optimization of LED light output and efficient supply of power to the LED’s. First, based on the LED characteristics and LED configuration different level of brightness could be obtained for the same amount of power. Hence, the term Luminous Efficiency which is defined as the ratio of luminous flux emitted from a light source to the electric power consumed by the source plays an important role governing overall efficiency. Second, an efficient conversion of the limited battery power to the useful form for LED’s to emit proper amount of light is of significant importance. This conversion of power is often achieved using voltage regulators as LED drivers and present enormous system and circuit level issues which have been a topic of interest to the researchers [1][2][3]. In general, LED luminance is found to be directly proportional to its drive current [4] and hence in some applications like backlight, and flash the desired LED brightness is achieved by controlling the LED drive. Under the condition where desired brightness cannot be obtained using a single LED, additional LEDs can be placed either in parallel or series [5]. Low power LED has been used for battery powered applications for decades [6][7][8]. These applications include cell phone handsets, digital still cameras, automotive lighting, emergency lighting, and LCD backlighting, and so on. With the advancement of new materials and manufacture process, a new lighting source, that is, high brightness white (HBW) LED is now attracting more and more
attention from industry [9][10][11][12]. This arrangement of multiple LEDs plays a significant role in defining the amount of current drained from the battery. In case of underground coal mines, mine workers are very much dependent on visual cues to recognize underground mining hazards. On the other hand, illumination plays a critical role in miners’ safety. Some hazards are located in the miners’ peripheral field-of-view off-axis (10° to about 60°) or on-axis (0°)[13]. Closed-loop buck-boost converter for driving LED has been designed in which output voltage of 12 V has been maintained and it is independent of input voltage and load change[14].

2. Analysis of Buck Boost Converter

![Figure 1. Equivalent Circuit for Buck boost Converter](image)

Figure 1. Equivalent Circuit for Buck boost Converter

![Figure 2. Equivalent Circuit for Buck boost Converter with switching operation](image)

Figure 2. Equivalent Circuit for Buck boost Converter with switching operation

![Figure 3. Buck boost Converter when switch is at position 1](image)

Figure 3. Buck boost Converter when switch is at position 1

![Figure 4. Buck boost Converter when switch is at position 2](image)

Figure 4. Buck boost Converter when switch is at position 2

A simple method for deriving the small-signal ac model of CCM (continuous current mode) converters is explained by Averaging Method. The switching ripples in the inductor current and capacitor voltage waveforms are removed by averaging over one switching period. Hence, the low-frequency components of the inductor and capacitor waveforms are modelled by equations of the form

\[
\begin{align*}
L \frac{di(t)}{dt} &= \langle v_L(t) \rangle T_s \\
C \frac{dv(t)}{dt} &= \langle i_C(t) \rangle T_s
\end{align*}
\]

(1)

Where \( \langle x(t) \rangle T_s \) denotes the average of \( x(t) \) over an interval of length \( T_s \). Let us derive a small-signal ac model of the buck-boost converter of Fig. 1. Let us consider \( R_L \) and \( R_C \) as the parasitic resistance of Inductor and Capacitor respectively. The analysis begins as usual, by determining the voltage and current waveforms of the inductor and capacitor. When the switch is in position 1, the circuit of Fig. 3 is obtained. The inductor voltage and capacitor current are given by,

\[
v_L(t) = L \frac{di(t)}{dt} = v_g(t) - R_L i(t) \tag{2}
\]

\[
i_C(t) = C \frac{dv(t)}{dt} = -\frac{v(t)}{R_L} \tag{3}
\]

We now make the small-ripple approximation. But rather than replacing \( v_g(t) \) and \( v(t) \) with their dc components \( V_g \) and \( V \) we now replace them with their low-frequency averaged values \( \langle v_g(t) \rangle T_s \) and \( \langle v(t) \rangle T_s \). Equations (2) and (3) becomes,

\[
v_L(t) = L \frac{di(t)}{dt} \approx \langle v_g(t) \rangle T_s - R_L \langle i(t) \rangle T_s \tag{4}
\]

\[
i_C(t) = C \frac{dv(t)}{dt} \approx -\frac{v(t)}{R} \tag{5}
\]

The inductor voltage and capacitor currents are

\[
v_L(t) = L \frac{di(t)}{dt} = v(t) - R_L i(t) \tag{6}
\]

\[
i_C(t) = C \frac{dv(t)}{dt} = -i(t) - \frac{v(t)}{R} \tag{7}
\]

Using the small ripple approximation to replace \( i(t) \) and \( v(t) \) with their averaged values,

\[
v_L(t) = L \frac{di(t)}{dt} \approx \langle v(t) \rangle T_s - R_L \langle i(t) \rangle T_s \tag{8}
\]
Similarly, averaging for input currents can be done.

\[ i_g(t) = \text{current drawn by converter from input source} \]

By neglecting the inductor current ripple and replacing \( i(t) \) with its averaged value \( \langle i(t) \rangle_{T_s} \), we can express the input current as follows:

\[ i_g(t) = \begin{cases} \langle i(t) \rangle_{T_s} & \text{during subinterval 1} \\ 0 & \text{during subinterval 2} \end{cases} \]

upon averaging over one switching period,

\[ \langle i_g(t) \rangle_{T_s} = d(t) \cdot \langle i(t) \rangle_{T_s} \]

From equations (11), (16) and (18) linearization can be done

\[ L \frac{d(i(t))_{T_s}}{dt} = d(t) \cdot \langle v_g(t) \rangle_{T_s} + d'(t) \cdot \langle v(t) \rangle_{T_s} - \frac{\langle v(t) \rangle_{T_s}}{R} \]

\[ \langle i_g(t) \rangle_{T_s} = d(t) \cdot \langle i(t) \rangle_{T_s} \]

Suppose that we drive the converter at some steady-state, or quiescent, duty ratio \( d(t) = D \), with quiescent input voltage \( v_g(t) = V_g \). From steady-state analysis, after any transients have subsided, the inductor current \( \langle i(t) \rangle_{T_s} \), the capacitor voltage \( \langle v(t) \rangle_{T_s} \) and the input current \( \langle i_g(t) \rangle_{T_s} \) will reach the quiescent values \( I \), \( V \), and \( I_g \) respectively, where

\[ V = -\frac{D}{D'} \cdot V_g \quad \text{and} \quad I = -\frac{V}{D' R} \quad \text{and} \quad I_g = DI \]

For small-signal ac model at quiescent operating point \((I,V)\), We assume that the input voltage \( v_g(t) \) and duty cycle \( d(t) \) are equal to quiescent values \( V_g \) and \( D \), plus some small ac variations \( v_g(t) \) and \( d(t) \).

\[ \langle v_g(t) \rangle_{T_s} = V_g + \delta v_g(t) \]

\[ d(t) = D + \delta d(t) \]
In response to these inputs and after any transients have subsided,

\[ i(t)_{rs} = I + \dot{i}(t) \]  

(23)

\[ v(t)_{rs} = V + \dot{v}(t) \]  

(24)

\[ i_g(t)_{rs} = I_g + \dot{i}_g(t) \]  

(25)

With the assumptions that the ac variations are small in magnitude compared to the dc quiescent values, or

\[ |\dot{v}_g(t)| \ll |V_g| \]
\[ |\dot{d}(t)| \ll |D| \]
\[ |\dot{i}(t)| \ll |I| \]  

(26)

\[ |\dot{v}(t)| \ll |V| \]

The non-linear equation (19) can be linearized by inserting equations (21), (22), (23) & (24) into equation (19).

\[
L \frac{d[l + \dot{i}(t)]}{dt} = [D + \dot{d}(t)] [V_g + \dot{v}_g(t)] + \\
[D' - \dot{d}(t)] [V + \dot{v}(t)] - R_L [I + \dot{i}(t)]
\]

(27)

It should be noted that complement of the duty cycle is given by,

\[ d'(t) = [1 - d(t)] = 1 - [D + \dot{d}(t)] = D' - \dot{d}(t) \]

(28)

Where \( D' = 1 - D \). By multiplying eqn.(27) and collecting terms,

\[
L \left[ \frac{d[l + \dot{i}(t)]}{dt} \right] = [D_0 V + D' V - R_L I] + \\
[D_0 \dot{v}_g(t) + D' \dot{v}(t) + (V_g - V) \dot{d}(t) - R_L \dot{i}(t)] + \\
\dot{d}(t) [\dot{v}_g(t) - \dot{v}(t)]
\]

(29)

The derivative of \( I \) is zero, since \( I \) is by definition a dc (constant) term. For the purposes of deriving a small-signal ac model, the dc terms can be considered known constant quantities. On the right-hand side of Eq. (25), three types of terms arise:

De terms: These terms contain dc quantities only.

First-order ac terms: Each of these terms contains a single ac quantity, usually multiplied by a constant coefficient such as a dc term. These terms are linear functions of the ac variations.

Second-order ac terms: These terms contain the products of ac quantities.

Hence they are nonlinear, because they involve the multiplication of time-varying signals. It is desired to neglect the nonlinear ac terms. Provided that the small-signal assumption, Eq. (22), is satisfied, then each of the second-order nonlinear terms is much smaller in magnitude that one or more of the linear first-order ac terms. We are left with the first-order ac terms on both sides of the equation.

\[ \Rightarrow L \frac{d[l + \dot{i}(t)]}{dt} = D_0 \dot{v}_g(t) + D' \dot{v}(t) + (V_g - V) \dot{d}(t) - R_L \dot{i}(t) \]

(30)

Insertion of eqn.(22), (23) and (24) into capacitor equation (19) yields,

\[
C \frac{d[V + \dot{v}(t)]}{dt} = \left[ \frac{-\frac{D_0 V}{R + R_C} - D' \dot{V}}{R + R_C} \right] + \\
\left[ \frac{-\frac{D \phi(t)}{R + R_C} - \frac{\dot{d}(t) V}{R + R_C}}{R + R_C} + D' \dot{v}(t) \right] - R_L \dot{i}(t) \]

(31)

\[ \Rightarrow C \frac{d[\dot{v}(t)]}{dt} = -\dot{v}(t) \left[ \frac{D' \dot{v}}{R + R_C} + \frac{D \dot{v}}{R + R_C} \right] + \dot{d}(t) \dot{v}(t) \left[ \frac{1}{R} \right] - \frac{1}{R + R_C} \left[ D' \dot{v}(t) + L \dot{d}(t) \right]
\]

(32)

This is the desired small-signal linearized equation that describes variations in the capacitor voltage.

Insertion of equation (22), (23) and (25) into equation (19) yields,

\[ I_g + \dot{i}_g(t) = [D + \dot{d}(t)][I + \dot{i}(t)] \]

(33)

By collecting terms, we obtain

\[ I_g + \dot{i}_g(t) = (DI) + [D\dot{i}(t) + I \dot{d}(t)] + \dot{d}(t) \dot{i}(t) \]
We again neglect the second-order nonlinear terms. The dc terms on both sides of the equation are equal. The remaining first-order linear ac terms are

\[ i_g(t) = D \dot{i}(t) + l \dot{d}(t) \] (34)

The small signal ac description of the buck boost converter with parasitic resistance are collected below:

\[ L \frac{d\hat{i}(t)}{dt} = D \hat{v}_g(t) + D' \hat{v}(t) + (V_g - V) \hat{d}(t) - R_L \hat{i}(t) \]

\[ L \frac{d\hat{v}(t)}{dt} = -\hat{v}(t) \left[ \frac{D'}{R} + \frac{D}{R + R_c} \right] + \hat{d}(t) V \left[ \frac{1}{R} - \frac{1}{R + R_c} \right] - D' \dot{i}(t) + l \dot{d}(t) \]

\[ i_g(t) = D \dot{i}(t) + l \dot{d}(t) \]

The converter contains two inputs \( \hat{d}(s) \) (control input) and \( \hat{v}_g(s) \) and one output \( \hat{v}(s) \).

Hence,

\[ \hat{v}(s) = G_{vd}(s) \hat{d}(s) + G_{vg}(s) \hat{v}_g(s) \]

Where \( G_{vd}(s) = \hat{v}(s)/\hat{d}(s) \) when \( \hat{v}_g(s) = 0 \)

\( G_{vg}(s) = \hat{v}(s)/\hat{v}_g(s) \) when \( \hat{d}(s) = 0 \)

Here, \( G_{vd}(s) \) is control-to-output transfer function.

and \( G_{vg}(s) \) is line-to-output transfer function.

By Laplace transform of converter equations, taking initial conditions as zero

\[ sL \hat{i}(s) = D \hat{v}_g(s) + D' \hat{v}(s) + (V_g - V) \hat{d}(s) - R_L \hat{i}(s) \]

\[ sC \hat{v}(s) = -D \dot{i}(s) + l \dot{d}(s) - \hat{v}(s) \frac{(R + D' R_c)}{R(R + R_c)} \hat{d}(s) + \hat{d}(s) V \left[ \frac{R_c}{R(R + R_c)} \right] \] (35)

Eliminating \( \hat{i}(s) \) and solving for \( \hat{v}(s) \)

\[ \hat{v}(s) = \frac{D \hat{v}_g(s) + D' \hat{v}(s) + (V_g - V) \hat{d}(s)}{sL + R_L} \] (36)

\[ \Rightarrow sC \hat{v}(s) + \hat{v}(s) \frac{(R + D' R_c)}{R(R + R_c)} = -D' \dot{i}(s) + l \dot{d}(s) + \hat{d}(s) V \left[ \frac{R_c}{R(R + R_c)} \right] \] (37)

\[ \Rightarrow \hat{v}(s) \left[ sC + \frac{R + D' R_c}{R(R + R_c)} + \frac{D'^2}{sL + R_L} \right] = -D \frac{\hat{v}_g(s)}{sL + R_L} + l \dot{d}(s) V \left[ \frac{R_c}{R(R + R_c)} \right] - D' \hat{d}(s) \] (38)

Equation (38) can also be written as,

\[ \Rightarrow \hat{v}(s) \left[ \frac{A_1 s^2 + A_2 s + A_3}{R(R + R_c)(sL + R_L)} \right] = -D \frac{\hat{v}_g(s)}{sL + R_L} + l \dot{d}(s) V \left[ \frac{R_c}{R(R + R_c)} \right] \] (39)

Where

\[ A_1 = (R + R_c) C R L \] (40)

\[ A_2 = L(R + D' R_c) + C R R_L (R + R_c) \] (41)

\[ A_3 = D'^2 R (R + R_c) + D' R_c R_L + R R_L \] (42)

\[ B_1 = I R L (R + R_c) + V R R_L \] (43)

\[ B_2 = I R R_L (R + R_c) + V R R_L - D' (V_g - V) R (R + R_c) \] (44)

\[ \Rightarrow \hat{v}(s) = \left[ -\frac{D D' R R_L}{A_1 s^2 + A_2 s + A_3} \right] \hat{v}_g(s) + \left[ \frac{B_1 s + B_2}{A_1 s^2 + A_2 s + A_3} \right] \hat{d}(s) \] (45)

Which is of the form

\[ \hat{v}(s) = G_{vd}(s) \hat{d}(s) + G_{vg}(s) \hat{v}_g(s) \]

Hence, control to output transfer function and line-to-output transfer function can be derived as

\[ G_{vd}(s) = \frac{B_1 s + B_2}{A_1 s^2 + A_2 s + A_3} \] (46)

\[ G_{vg}(s) = -\frac{D D' R R_L}{A_1 s^2 + A_2 s + A_3} \] (47)
Values of $A_1, A_2, A_3, B_1$ and $B_2$ can be calculated with the help of equations (40), (41), (42), (43) and (44) respectively.

3. Closed Loop Transfer Function of Buck Boost Converter Based Control System

Figure 5. Block Diagram of closed loop buck boost converter based control system

From the above block diagram, it can be written as,

$$\bar{v}_e = V_{ref} - H(s)\bar{v}(s)$$  \hspace{1cm} (48)

$$\bar{v}_{ctrlo} = C(s)\bar{v}_e$$ \hspace{1cm} (49)

$$\hat{d}(s) = \bar{v}_{ctrlo} \cdot \frac{1}{V_P}$$ \hspace{1cm} (50)

$$\bar{v}(s) = \hat{d}(s) G_{vd}(s)$$ \hspace{1cm} (51)

Hence, From above equations,

$$\frac{\bar{v}(s)}{V_{ref}} = \frac{C(s) G_{vd}(s)}{V_P + C(s) H(s) G_{vd}(s)}$$ \hspace{1cm} (52)

Equation (52) shows the closed loop transfer function of the buck-boost converter. Here, $C(s)$ is the transfer function of Voltage Stabilize. $H(s)$ is the transfer function of Voltage divider.

$$\frac{1}{V_P}$$ is the transfer function of PWM.

Figure 6. Control circuit for the system

$$C(s) = \frac{1}{R_1 R_1 C_1} \cdot \frac{1}{s \left[ s + \frac{R_2 C_2}{R_1 C_1 C_2} \right]}$$ \hspace{1cm} (53)

Take, $H(s) = \frac{1}{K}$ \hspace{1cm} (54)

Hence,

$$\frac{\bar{v}(s)}{V_{ref}} = \frac{K[B_1 R_2 C_2 s^2 + (B_1 + B_2 R_2 C_2) s + B_2]}{Q_4 s^4 + Q_3 s^3 + Q_2 s^2 + Q_1 s + 1}$$ \hspace{1cm} (55)

In equation (55),

$$Q_4 = V_p \cdot K \cdot R_1 R_2 C_1 C_2 \cdot A_1$$ \hspace{1cm} (56)

$$Q_3 = V_p \cdot K [A_2 R_1 R_2 C_1 C_2 + A_1 (C_1 + C_2) R_2]$$ \hspace{1cm} (57)

$$Q_2 = V_p \cdot K [A_3 R_1 R_2 C_1 C_2 + A_2 (C_1 + C_2) R_2]$$ \hspace{1cm} (58)

$$Q_1 = V_p \cdot K [A_3 (C_1 + C_2) R_2 + R_2 \cdot C_2]$$ \hspace{1cm} (59)

4. Result and Discussion

Table 1:

<table>
<thead>
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<th>parameter</th>
<th>value</th>
<th>parameter</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R$</td>
<td>2.4 ohms</td>
<td>$R_L$</td>
<td>5 ohm</td>
</tr>
<tr>
<td>$L$</td>
<td>0.01H</td>
<td>$R_C$</td>
<td>5 ohm</td>
</tr>
<tr>
<td>$C$</td>
<td>0.5 F</td>
<td>$C_3$</td>
<td>81.1058mF</td>
</tr>
<tr>
<td>$V_{in}$</td>
<td>8 V</td>
<td>$V_o$</td>
<td>12 V</td>
</tr>
<tr>
<td>Duty ratio</td>
<td>0.6</td>
<td>$R_2$</td>
<td>2.86726ohms</td>
</tr>
</tbody>
</table>

Based on the parameter of different components as mentioned in table 1 the transfer function of converter and overall system has been calculated and bode plot has been plotted by using MATLAB. In the other way depending upon the nature of regulator and type of converter the transfer function has been obtained by PSIM. Finally, the performance of regulator, converter and overall system has been observed as stable. Figure 7 to Figure 12 shows the nature of bode plot obtained with the help of MATLAB and PSIM.
Figure 7. Bode plot of regulator by MATLAB

Figure 8. Bode plot (magnitude) of regulator by PSIM

Figure 9. Bode plot (phase) of regulator by PSIM

Figure 10. Bode plot (phase) of overall transfer function by PSIM

Figure 11. Bode plot (magnitude) of overall transfer function by PSIM

Figure 12. Bode plot of overall transfer function by MATLAB

Figure 13. Output Current waveform.

Figure 14. Output Current with sudden change in load.

Figure 15. Output Current with sudden change in supply voltage.
5. Prototype Developments

It is observed that for a load of 20 Ohms, a constant current of 600mA is obtained. Fig. 13 shows the constant current waveform while Fig. 14 shows current with sudden change in load and Fig. 15 shows current with sudden change in supply voltage. The prototype for buck boost switch based closed loop has been designed for a power rating of 10W with 10V output at 100 KHz switching frequency in CCM operation using microcontroller IC number 8951 based PWM and efficiency has been observed as 80% with ripple value of 0.02%. The system has been tested for 20% change of load. The system has been tested for 12 hours to check the performance of the system.

6. Conclusion

Based on the result obtained from the system it has been observed that LED has been illuminated for constant intensity. The phase margin of the buck boost converter and whole driver circuit has been observed as 93.206° and 93.8° respectively making system as stable and suitable for typical environmental scenario.

References


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