Hybrid BFOA-PSO Approach for Robust Design of TCSC Based Controller

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Abstract: Social foraging behaviour of Escherichia coli bacteria has recently been explored to develop a novel algorithm for optimization and control. One of the major driving forces of Bacterial Foraging Optimization Algorithm (BFOA) is the chemotactic movement of a virtual bacterium that models a trial solution of the optimization problem. However, during the process of chemotaxis, the BFOA depends on random search directions which may lead to delay in reaching the global solution. This paper comes up with a hybrid approach involving Particle Swarm Optimization (PSO) and BFOA algorithm called Bacterial Swarm Optimization (BSO) for designing Thyristor Controlled Series Capacitor (TCSC) in a multimachine power system. In BSO, the search directions of tumble behaviour for each bacterium are oriented by the individual’s best location and the global best location of PSO. The proposed hybrid algorithm has been extensively compared with BFOA and PSO. Simulation results have shown the validity of the proposed BSO in tuning TCSC compared with BFOA and PSO. Moreover, the results are presented to demonstrate the effectiveness of the proposed controller to improve the power system stability over a wide range of loading conditions.

Key-Words: - TCSC; Multimachine Power System; Particle Swarm Optimization; Bacterial Foraging; Hybrid Algorithm; Damping Oscillations.

1. Introduction

The power transfer in an integrated power system is constrained by transient stability, voltage stability and small signal stability. These constraints limit a full utilization of available transmission corridors. Flexible AC Transmission System (FACTS) is the technology that provides the needed corrections of the transmission functionality in order to fully utilize the existing transmission facilities and hence, minimizing the gap between the stability limit and thermal limit [1].

Thyristor controlled series compensator (TCSC) is one of the important members of FACTS family that is increasingly applied by the utilities in modern power systems with long transmission lines. It has various roles in the operation and control of power systems, such as scheduling power flow; reducing net loss; providing voltage support; limiting short circuit currents; mitigating sub-synchronous resonance (SSR); damping the power oscillations; and enhancing transient stability [2]. The applications of TCSC for power oscillations damping and stability enhancement can be found in [3-6].

In last few years, many researchers have posed techniques for designing TCSC to enhance the damping of electromechanical oscillations of power systems and application of different optimization techniques in improving power system stability. The power system stability enhancement via power system stabilizer (PSS) and TCSC based stabilizer when applied independently and also through coordinated application is investigated in [7]. A procedure for modelling and tuning the parameters of TCSC compensation controller in a multimachine power system to improve system stability using (genetic algorithm) GA is introduced in [8]. To eliminate the disadvantage of GAs, a new optimization scheme known as bacterial foraging (BF) is used for the PSS parameter design in a multimachine system [9]. The application and performance comparison of particle swarm optimization (PSO) and GA techniques, for FACTS based controller design is discussed in [10]. A supplementary damping control system design for TCSC based on natural inspired Virtual Bees Algorithm (VBA) is presented in [11]. A new design procedure for simultaneous coordination designing of the TCSC damping controller and PSS in multimachine power system is developed in [12] using PSO. Coordination of TCSC controllers is conducted by applying a linear matrix inequality is illustrated in [13]. An efficient parallel GA (EPGA) for the solution of large scale optimal power flow problems to reduce the high CPU time execution is designed in [14]. A reduced rule base self-tuning fuzzy PI controller (STFPIC) for TCSC is discussed in [15]. The parameter tuning of a PID controller for a FACTS based stabilizer employing multi-objective evolutionary algorithm is introduced in [16].

Several optimization techniques have been adopted to solve a variety of engineering problems in the past decade. GA has attracted the attention in the field of controller parameter optimization. Although GA is very satisfactory in finding global or near global optimal result of the problem; it needs a very long run time that may be several minutes or even several hours depending on the size of the system under study. Moreover swarming strategies in bird flocking and fish schooling are used in the PSO and introduced in [17]. However, PSO suffers from the partial optimism, which causes the less exact at the regulation of its speed and the direction. Also, the algorithm cannot work out the problems of scattering and optimization [18-19]. In addition, the algorithm pains from slow convergence in refined...
search stage, weak local search ability and algorithm may lead to possible entrapment in local minimum solutions. A relatively newer evolutionary computation algorithm, called BF scheme has been addressed by [20-22] and further established recently by [23-24]. The BF algorithm depends on random search directions which may lead to delay in reaching the global solution. A new algorithm BF is oriented by PSO is developed that combine the above mentioned optimization algorithms [25-26]. This combination aims to make use of PSO ability to exchange social information and BF ability in finding a new solution by elimination and dispersal. This new hybrid algorithm called Bacterial Swarm Optimization (BSO) is adopted in this paper to solve the above mentioned problems and drawbacks.

This paper proposes a new optimization algorithm known as BSO for optimal design of the TCSC damping controller in a multimachine power system to damp power system oscillations. The performance of BSO has been compared with those of PSO and BFOA in tuning the TCSC damping controller parameters. The design problem of the proposed controller is formulated as an optimization problem and BSO is employed to search for optimal controller parameters. An eigenvalue based objective function reflecting the combination of damping factor and damping ratio is optimized for different operating conditions. Simulation results assure the effectiveness of the proposed controller in providing good damping characteristic to system oscillations over a wide range of loading conditions. Also, these results validate the superiority of the proposed method in tuning controller compared with BFOA and PSO.

2. Problem Statement
2.1 Power System Model

A power system can be modelled by a set of nonlinear differential equations as:

\[ \dot{X} = f(X, U) \]  

(1)

Where \( X \) is the vector of the state variables and \( U \) is the vector of input variables. In this study \( X = [\delta, \omega, E'_q, E_{fd}, V_f]^T \) and \( U \) is the TCSC output signal. Here, \( \delta \) and \( \omega \) are the rotor angle and speed, respectively. Also, \( E'_q, E_{fd} \) and \( V_f \) are the internal, the field, and excitation voltages respectively.

In the design of TCSC, the linearized incremental models around an equilibrium point are usually employed. Therefore, the state equation of a power system with \( n \) machines and \( m \) TCSC can be written as:

\[ \dot{X} = AX + BU \]  

(2)

Where \( A \) is a \( 5n \times 5n \) matrix and equals \( \partial \dot{\delta} / \partial X \) while \( B \) is a \( 5n \times m \) matrix and equals \( \partial \dot{\delta} / \partial U \). Both \( A \) and \( B \) are evaluated at a certain operating point. \( X \) is a \( 5n \times 1 \) state vector and \( U \) is a \( m \times 1 \) input vector.

Fig. 1 shows the single line diagram of the system under study. Details of system data are given in [27]. The participation matrix can be used in mode identification. Table (1) shows the eigenvalues, and frequencies associated with the rotor oscillation modes of the system. Examining Table (1) indicates that the \( 0.2371 \) Hz mode is the interarea mode with G1 swinging against G2 and G3. The \( 1.2955 \) Hz mode is the intermachine oscillation local to G2. Also, the \( 1.8493 \) Hz mode is the intermachine mode local to G3. The positive real part of eigenvalue of G1 indicates instability of the system. The system and generator loading levels are given in Table (2).

![Fig. 1. System under study.](image)

<table>
<thead>
<tr>
<th>Generator</th>
<th>Eigenvalues</th>
<th>Frequencies (Hz)</th>
<th>Damping ratio ( \zeta )</th>
</tr>
</thead>
<tbody>
<tr>
<td>G1</td>
<td>+0.15 ± 1.49j</td>
<td>0.2371</td>
<td>-0.1002</td>
</tr>
<tr>
<td>G2</td>
<td>-0.35 ± 8.14j</td>
<td>1.2955</td>
<td>0.0430</td>
</tr>
<tr>
<td>G3</td>
<td>-0.67 ± 11.62</td>
<td>1.8493</td>
<td>0.0576</td>
</tr>
</tbody>
</table>

Table (2) Loading of the system (in p.u)

<table>
<thead>
<tr>
<th>Generator</th>
<th>Load</th>
<th>Normal case</th>
<th>Heavy</th>
</tr>
</thead>
<tbody>
<tr>
<td>G1</td>
<td>A</td>
<td>P</td>
<td>P</td>
</tr>
<tr>
<td></td>
<td>B</td>
<td>Q</td>
<td>Q</td>
</tr>
<tr>
<td></td>
<td>C</td>
<td>P</td>
<td>P</td>
</tr>
<tr>
<td></td>
<td>at G1</td>
<td>0.6</td>
<td>0.2</td>
</tr>
</tbody>
</table>

Table (1) The eigenvalues, and frequencies of the rotor oscillation modes of the system.
2.2 TCSC Modelling and Damping Controller Design

A typical TCSC module consists of a fixed series capacitor in parallel with a thyristor controlled reactor (TCR). The TCR is formed by a reactor in series with a bi-directional thyristor valve which is fired by a phase angle $\alpha$ ranging between 90 and 180° with respect to the capacitor voltage. For the load flow and dynamic stability analysis studies, a TCSC can be modelled as a variable reactance. The dynamic equation of TCSC reactance can be expressed as following:

$$\Delta X_{TCSC} = \frac{1}{T_s}(K_s(\Delta X_{TCSC}^{ref} + \Delta U_{TCSC}) - \Delta X_{TCSC})$$  (3)

Where $X_{TCSC}^{ref}$ is the reference reactance of the TCSC; $K_s$ and $T_s$ are the gain and time constant of TCSC.

The structure of the TCSC based damping controller is shown in Fig. 2. The parameters of the damping controllers are obtained using various optimization algorithms. Many input signals have been proposed for the FACTS to damp the system oscillations. Signals which carry invaluable information about the interarea mode can be considered as the input signals. Since FACTS controllers are located in the transmission systems, local input signals are always preferred. For example, line active power and current carry such valuable information. Transmission line active power has been proposed as an effective input signal in [16, 17] for series FACTS devices damping controller design. For this reason, here, the active power of the transmission line is selected as the input signal. The line flow data are given in Table (3). The power flow in line 5-7 is the largest power flow in the system under study. Moreover, this line is the longest line in the system. So, one will consider this line as the best location for installing the TCSC controller in this paper. The TCSC parameters are given in Appendix.

$$J_t = \sum_{j=1}^{np} \sum_{i=1}^{np} (\sigma_{ij} - \sigma_0)^2 + \sum_{j=1}^{np} (\xi_{ij} - \xi_0)^2$$  (4)

This will place the system closed loop eigenvalues in the D-shape sector as shown in Fig. 3.

$$\sigma_{ij} \leq \sigma_0$$ and $$\xi_{ij} \geq \xi_0$$

Fig. 3. A D-shape sector in the s-plane.

Table (3) Base case (line flow) on 100 MVA base.

<table>
<thead>
<tr>
<th>From bus</th>
<th>To bus</th>
<th>Real power (p.u)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
<td>6</td>
<td>0.3070</td>
</tr>
<tr>
<td>6</td>
<td>9</td>
<td>0.6082</td>
</tr>
<tr>
<td>4</td>
<td>5</td>
<td>0.4094</td>
</tr>
<tr>
<td>5</td>
<td>7</td>
<td>0.8662</td>
</tr>
<tr>
<td>7</td>
<td>8</td>
<td>0.7638</td>
</tr>
<tr>
<td>8</td>
<td>9</td>
<td>0.2410</td>
</tr>
</tbody>
</table>

3. Objective Function

To maintain stability and provide greater damping, the parameters of the TCSC may be selected to minimize the following objective function [28]:

Where $\sigma_0$ and $\xi_0$ are chosen to be -0.5 and 0.10 respectively. To reduce the computational burden in this study, the value of the wash out time constant $T_W$ is fixed to 10 second, and the values of $T_2$ and $T_4$ are kept constant at a reasonable value of 0.05 second and tuning of $T_1$ and $T_3$ are undertaken to achieve the net phase lead required by the system. Typical ranges of the optimized parameters are [0.01-50] for $K$ and [0.01-1.0] for $T_1$ and $T_3$. Based on the objective function $J_t$ optimization problem can be stated as: Minimize $J_t$ subjected to:

$$K_{min} \leq K \leq K_{max}$$
The number of bacteria in population, \( t \), respectively.

\[
T_1^m \leq T_i \leq T_1^m
\]

\[
T_3^m \leq T_3 \leq T_3^m
\]

(5)

### 4. Hybrid BFOA-PSO Optimization Algorithm

PSO is a stochastic optimization technique that draws inspiration from the behaviour of a flock of birds or the collective intelligence of a group of social insects with limited individual capabilities. In PSO a population of particles is initialized with random positions \( X_i \) and velocities \( V_i \), and a fitness function using the particle’s positional coordinates as input values. Positions and velocities are adjusted, and the function is evaluated with the new coordinates at each time step \([17]\). The velocity and position update equations for the \( d \)-th dimension of the \( i \)-th particle in the swarm may be given as follows:

\[
V_{id}(t+1) = \omega \cdot V_{id}(t) + \theta 

\]

\[
X_{id}(t) + \phi 

\]

\[
C(d) \Delta T_{gd}(t) \]

(6)

(7)

Where \( X_{gd} \) is the best position of each bacterial and \( X_{gd} \) is the global best bacterial.

On the other hand, the BF is based upon search and optimal foraging decision making capabilities of the Escherichia coli bacteria \([25]\). The coordinates of a bacterium here represent an individual solution of the optimization problem. Such a set of trial solutions converges towards the optimal solution following the foraging group dynamics of the bacteria population. Chemotactic movement is continued until a bacterium goes in the direction of positive nutrient gradient. After a certain number of complete swims the best half of the population undergoes reproduction, eliminating the rest of the population. In order to escape local optima, an elimination dispersion event is carried out where, some of the population. In order to escape local optima, an elimination dispersion event is carried out where, some bacteria are liquidated at random with a very small probability and the new replacements are initialized at random locations of the search space. A detailed description of the complete algorithm can be traced in \([25-26]\). Also, the flow charts of PSO, BFOA, and BSO are shown in figs. 4-6 respectively. 

[Step 1] Initialize parameters

\( n, S, N_C, N_S, N_{re}, N_{ed}, P_{ed}, C(i)(i=1,2,\ldots,N),\phi \).

Where,

\( n \): Dimension of the search space,

\( S \): The number of bacteria in population,

\( N_{re} \): The number of reproduction steps,

\( N_C \): The number of chemotactic steps,

\( N_S \): Swimming length after which tumbling of bacteria is performed in a chemotaxis loop,

\( N_{ed} \): The number of elimination-dispersal events to be imposed over the bacteria,

\( P_{ed} \): The probability with which the elimination and dispersal will continue,

\( C(i) \): The size of the step taken in the random direction specified by the tumble,

\( \omega \): The inertia weight,

\( C_1, C_2 \): The swarm confidence,

\( \theta (i,j,k) \): Position vector of the \( i \)-th bacterium, in \( j \)-th chemotactic step and \( k \)-th reproduction,

\( V_i \): Velocity vector of the \( i \)-th bacterium.

[Step 2] Update the following

\( J(i,j,k) \): Cost or fitness value of the \( i \)-th bacterium in the \( j \)-th chemotaxis, and the \( k \)-th reproduction loop.

\( \theta \): Position vector of the best position found by all bacteria.

\( J_{best}(i,j,k) \): Fitness value of the best position found so far.

[Step 3] Reproduction loop: \( k = k + 1 \)

[Step 4] Chemotaxis loop: \( j = j + 1 \)

[Sub step a] For \( i = 1, 2, \ldots, S \), take a chemotaxis step for bacterium \( i \) as follows.

[Sub step b] Compute fitness function, \( J(i,j,k) \).

[Sub step c] Let \( J_{last} = J(i,j,k) \) to save this value since one may find a better cost via a run.

[Sub step d] Tumble: generate a random vector \( \Delta(i) \in \mathbb{R}^d \) with each element \( \Delta_m(i), m = 1,2,\ldots,n \), a random number on \([-1,1]\).

[Sub step e] Move:

\( \theta(i,j+1,k) = \theta(i,j,k) + C(i) \frac{\Delta(i)}{\sqrt{\Delta^T(i)\Delta(i)}} \).

[Sub step f] Compute \( J(i,j+1,k) \).

[Sub step g] Swim: one considers only the \( i \)-th bacterium is swimming while the others are not moving then

i) Let \( m = 0 \) (counter for swim length).

ii) While \( m < N_S \) (have not climbed down too long)

   - Let \( m = m + 1 \)

   - If \( J(i,j + 1,k) < J_{last} \) (if doing better),
Let \( J_{last} = J(i, j+1, k) \) and let
\[
\theta(i, j+1, k) = \theta(i, j, k) + C(i) \frac{\Delta(i)}{\sqrt{\Delta^T(i)\Delta(i)}}
\]
and use this \( \theta(i, j+1, k) \) to compute the new \( J(i, j+1, k) \) as shown in new [sub step f]
• Else, let \( m = N_S \). This is the end of the while statement.

[Step 5] Mutation with PSO operator
For \( i = 1, 2, \ldots, S \)
• Update the \( \theta_{g_best} \) and \( J_{best}(i, j, k) \)
• Update the position and velocity of the \( d \)-th coordinate of the \( i \)-th bacterium according to the following rule:
\[
y_{new}^{id} = c_0 \theta_{new}^{id} + C_i \theta_{g_best}^{id} - \theta_{old}^{id}(i, j+1, k)
\]
\[
\theta_{new}^{d}(i, j+1, k) = \theta_{old}^{d}(i, j+1, k) + y_{new}^{id}
\]

[Step 6] Let \( S_r = S / 2 \)
The \( S_r \) bacteria with highest cost function \( (J) \) values die and other half bacteria population with the best values split.

Fig. 4. Flow chart of PSO algorithm.

[Step 7] If \( k < N_{re} \), go to [step 3]. One has not reached the number of specified reproduction steps, so one starts the next generation in the chemotaxis loop.

More details of BFOA and PSO parameters are presented in Appendix.
5. Results and Simulations

In this section, the superiority of the proposed BSO algorithm in designing TCSC (BSOTCSC) in compare to optimized TCSC with PSO (PSOTCSC) and optimized TCSC controller based on BFOA (BFTCSC) is illustrated.

Fig. 7. shows the variations of objective function with different optimization techniques. The objective functions decrease monotonically over generations of BFOA, PSO and BSO. The final value of the objective function is zero for all algorithms, indicating that all modes have been shifted to the specified D-shape sector in the S-plane and the proposed objective function is satisfied. Moreover, BSO converges at a faster rate (45 generations) compared to that for PSO (61 generations) and BFOA (82 generations).

Computational time (CPU) of all algorithms is compared based on the average CPU time taken to converge the solution. The average CPU for BSO is 26.84 second while it is 34.28 and 42.56 second for PSO and BFOA respectively. It is clear that, average convergence time for BSO is less than other methods. The higher computational time for BFOA is expected due to its dependence on random search directions which may lead to delay in reaching the global solution. On the other hand, PSO suffers from the partial optimism, which causes the less exact at the regulation of its speed and the direction. In addition, the algorithm pains from slow convergence in refined search stage, weak local search ability and algorithm may lead to possible entrapment in local minimum solutions.

Table (4), shows the system eigenvalues, and damping ratio of mechanical mode with three different loading conditions. It is clear that the BSOTCSC shift substantially the electromechanical mode eigenvalues to the left of the S-plane and the values of the damping factors with the proposed BSOTCSC are significantly improved to be ($\sigma =-0.74,-0.75,-0.98$) for light, normal, and heavy loading respectively. Also, the damping ratios corresponding to BSOTCSC controllers are almost greater than those corresponding to PSOTCSC and BFTCSC ones. Hence, compared to BFTCSC and PSOTCSC, BSOTCSC greatly enhances the system stability and improves the damping characteristics of electromechanical modes. Results of TCSC parameters set values based on the proposed objective function using BSO, PSO, and BFOA are given in Table (5).
Table (4) Mechanical modes and $\zeta$ under different loading conditions and controllers.

<table>
<thead>
<tr>
<th>Mode</th>
<th>Light load</th>
<th>Normal load</th>
<th>Heavy load</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\omega_{12}$</td>
<td>$-3.99 \pm 9.12j, 0.40$</td>
<td>$-3.39 \pm 11.2j, 0.29$</td>
<td>$-3.81 \pm 11.5j, 0.31$</td>
</tr>
<tr>
<td>$\omega_{13}$</td>
<td>$-3.96 \pm 9.25j, 0.39$</td>
<td>$-3.27 \pm 11.3j, 0.28$</td>
<td>$-3.45 \pm 11.4j, 0.29$</td>
</tr>
<tr>
<td>$\zeta$</td>
<td>$0.31 \pm 0.64j, 0.20$</td>
<td>$0.73 \pm 0.76j, 0.09$</td>
<td>$0.79 \pm 0.79j, 0.78$</td>
</tr>
</tbody>
</table>

Table (5) Parameters of TCSC damping controller.

<table>
<thead>
<tr>
<th>Controller</th>
<th>$K$</th>
<th>$T_1$</th>
<th>$T_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>BSOTCSC</td>
<td>4.2531</td>
<td>0.6754</td>
<td>0.2859</td>
</tr>
<tr>
<td>PSOTCSC</td>
<td>3.2459</td>
<td>0.5348</td>
<td>0.2516</td>
</tr>
<tr>
<td>BFTCSC</td>
<td>2.9155</td>
<td>0.3384</td>
<td>0.1252</td>
</tr>
</tbody>
</table>

5.1 Response under normal load condition:
The effectiveness of the performance under severe disturbance is verified by applying a three phase fault of 6 cycle duration at 1.0 second near bus 2. Fig. 8 shows the response of $\Delta \omega_{12}$ for normal loading condition. This figure indicates the capability of the BSOTCSC in reducing the settling time and damping power system oscillations. Moreover, the mean settling time of these oscillations is 4.4, 6.1, and 7.0 second for BSOTCSC, PSOTCSC, and BFTCSC respectively. In addition, the proposed BSOTCSC outperforms and outlasts PSOTCSC and BFTCSC controller in damping oscillations effectively and reducing settling time.

Fig. 8. Response of $\Delta \omega_{12}$ for normal load condition.

5.2 Response under heavy load condition:
Fig. 9 shows the system response at heavy loading condition with fixing the controller parameters. From this figure, it can be seen that the response with the proposed BSOTCSC shows good damping characteristics to low frequency oscillations and the system is more quickly stabilized than PSOTCSC and BFTCSC. The mean settling time of oscillation is 5.6, 9.4, and 13.1 second for BSOTCSC, PSOTCSC, and BFTCSC respectively. Hence, the proposed BSOTCSC extend the power system stability limit.

Fig. 9. Response of $\Delta \omega_{13}$ for heavy load condition.

5.3 Robustness and performance index:
To demonstrate the robustness of the proposed controller, a performance index: the Integral of the Time multiplied Absolute value of the Error (ITAE) is being used as:

$$ITAE = \frac{30}{T} \int_0^T (|\Delta \omega_{12}| + |\Delta \omega_{23}| + |\Delta \omega_{13}|)dt$$  \(8\)

Where $\Delta \omega_{12} = \omega_1 - \omega_2$, $\Delta \omega_{23} = \omega_2 - \Delta \omega_3$, and $\Delta \omega_{13} = \omega_1 - \Delta \omega_3$. It is worth mentioning that the lower the value of this index is, the better the system response in terms of time domain characteristics. Numerical results of performance robustness for all cases are listed in Table (6). It can be seen that, the values of these system performance characteristics with the proposed BSOTCSC are smaller compared to those of PSOTCSC and BFTCSC. This demonstrates that the overshoot, undershoot; settling time, and speed deviations of all units are greatly reduced by applying the proposed BSOTCSC controller.

Table (6) Values of performance index.

<table>
<thead>
<tr>
<th>Controller</th>
<th>ITAE</th>
</tr>
</thead>
<tbody>
<tr>
<td>BSOTCSC</td>
<td>0.0029</td>
</tr>
<tr>
<td>PSOTCSC</td>
<td>0.0037</td>
</tr>
<tr>
<td>BFTCSC</td>
<td>0.0042</td>
</tr>
</tbody>
</table>

6. Conclusions
In this study, a new optimization algorithm known as BSO, which synergistically couples the BFOA with the PSO for optimal designing of TSC damping controller is thoroughly investigated. For the proposed controller design problem, an eigenvalue based objective function reflecting the combination of
damping factor and damping ratio to minimize the power system oscillations is used. Simulation results are presented for various loading conditions to verify the effectiveness of the proposed controller design approach. Moreover, the system performance characteristics in terms of ‘ITAE’ index reveal that the proposed PSOTCSC and BFTCSC at various operating conditions. Finally, the proposed control scheme is robust, simple to implement, yet valid over a wide range of operating conditions.

7. References

Appendix
The system data are as shown below:

a) Excitation system: \( K_A = 400; \ T_A = 0.05 \text{ second}; \ K_f = 0.025; \ T_f = 1 \text{ second}. \)

b) TCSC Controller: \( T_s = 0.015 \text{ second}; \text{ firing angle} \ (\alpha) \approx 147.5; \ K_h = 50; \)

c) Bacteria parameters: Number of bacteria \(= 10; \) number of chemotactic steps \(= 10; \) number of elimination and dispersal events \(= 2; \) number of reproduction steps \(= 4; \) probability of elimination and dispersal \(= 0.25; \text{ the values of } d_{\text{attract}} = 0.01; \text{ the values of } d_{\text{repelent}} = 0.04; \text{ the values of } h_{\text{attract}} = -0.01; \text{ the values of } h_{\text{repelent}} = -0.10. \)

d) PSO parameters: \( C_1 = C_2 = 2.0; \) \( \alpha = 0.9. \)